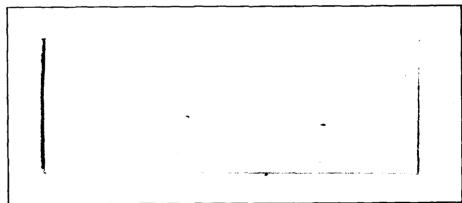
YALE UNIV NEW HAVEN CT DEPT OF COMPUTER SCIENCE F/6 9/ IMPOSSIBILITY OF DISTRIBUTED CONSENSUS WITH ONE FAULT PROCESS.(U) SEP 82 M J FISCHER, M A LYNCH, M S PATERSON NODD14-82-K-0154 RR-245 40-A120 161 F/6 9/2 UNCLASSIFIED NL 10:1 END DATE 11.82 DTI€









E

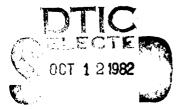
YALE UNIVERSITY
DEPARTMENT OF COMPUTER SCIENCE

This decrees the closed approved for pathing a second sales its distribution is autonited.

# IMPOSSIBILITY of DISTRIBUTED CONSENSUS with ONE FAULTY PROCESS\*

Ъy

Michael J. Fischer, Nancy A. Lynch and Michael S. Paterson Research Report # 245 September 1982



E

l'alua disservation de la companie de la distribution us villament.

REPORT DOCUMENTATION PAGE	READ INSTRUCTIONS BEFORE COMPLETING FORM
1. REPORT NUMBER 2. GOVT ACCESSION NO.	3. RECIPIENT'S CATALOG NUMBER
245 21 AD-A120161	
4. TITLE (and Subtitle)	S. TYPE OF REPORT & PERIOD COVERED
IMPOSSIBILITY OF DISTRIBUTED CONSENSUS WITH ONE FAULTY PROCESS*	Technical Report
	6. PERFORMING ORG. REPORT NUMBER
7. AUTHOR(e)	B. CONTRACT OF GRANT NUMBER(a) ONR: NO0014-82-K-0154; ARO:
Michael J. Fischer, Nancy A. Lynch and	DAAG29-79-C-0155 and NSF:
Michael S. Paterson	MCS-7924370 and MCS-8116678
PERFORMING ORGANIZATION NAME AND ADDRESS  Department of Computer Science/Yale University	10. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS
Dunham Lab./10 Hillhouse Avenue New Haven, Connecticut 06520	NR 049-456/11-5-81 410
11. CONTROLLING OFFICE NAME AND ADDRESS	12. REPORT DATE
NSF, Washington, D.C. 20550/Office of Naval	September, 1982
Research, 800 N. Quincy, Arlington, VA 22217/ U.S. Army Research Office, P.O.Box 12211,	13. NUMBER OF PAGES
Research Triangle Park, NC 27709 14. MONITORING AGENCY NAME & ADDRESS(II dillorum) trum Controlling Office)	14
14. MONITORING AGENCY NAME & ADDRESS(II dillorent from Controlling Office) Office of Naval Research	18. SECURITY CLASS. (of this report)
800 N. Quincy	Unclassified
Arlington, VA 22217	The DECLASSIFICATION/DOWNGRADING
ATTN: Dr. R.B. Grafton	184. DECLASSIFICATION/DOWNGRADING SCHEDULE
Approved for public release; distributed unlimited.	
17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different from Report)	
,	
18. SUPPLEMENTARY NOTES	<del></del>
19. KEY WORDS (Continue on reverse side if necessary and identify by block mamber)	
Distributed commit problem, distributed coordination, fault-tolerance,	
protocols, distributed systems.	
N	
20. VABSTRACT (Continue on reverse olde if necessary and identify by block number)	
The consensus problem involves an asynchronous sytem of processes, some of which may be unreliable. The problem is for the reliable processes to agree	

on a binary value. We show that every protocol for this problem has the possibility of nontermination, even with only one faulty process. By way of contrast, solutions are known for the synchronous case, the "Byzantine

DD 1 JAN 73 1473 EDITION OF 1 NOV 65 IS OBSOLETE S/N 0102-LF-014-6601

Generals" problem.

SECURITY CLASSIFICATION OF THIS PAGE (Then Date Entered)

## Impossibility of Distributed Consensus with One Faulty Process\*

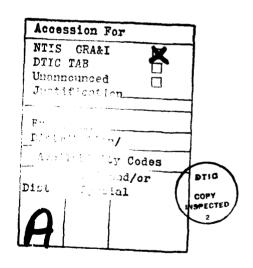
Michael J. Fischer Yale University New Haven, Connecticut

Nancy A. Lynch
Massachusetts Institute of Technology
Cambridge, Massachusetts
(on leave from Georgia Institute of Technology)

and

Michael S. Paterson University of Warwick Coventry, England

September 1982



<sup>a</sup>This work was supported in part by the Office of Naval Research under Contract N00014-82-K-0154, by the Office of Army Research under Contract DAAG29-79-C-0155, and by the National Science Foundation under Grants MCS-7924370 and MCS-8116678.

### ABSTRACT

The consensus problem involves an asynchronous system of processes, some of which may be unreliable. The problem is for the reliable processes to agree on a binary value. We show that every protocol for this problem has the possibility of nontermination, even with only one faulty process. By way of contrast, solutions are known for the synchronous case, the "Byzantine Generals" problem.

### 1. Introduction

The problem of reaching agreement among remote processes is one of the most fundamental problems in distributed computing. It is at the core of many of algorithms for distributed data processing, distributed file management, and fault-tolerant distributed applications.

A well-known form of the problem is the "transaction commit problem" which arises in distributed database systems [DS1, G, LS, La, Le, Li, R, RLS, S, SS]. The problem is for all the data manager processes which have participated in the processing of a particular transaction to agree on whether to install the transaction's results in the database or to discard them. The latter action might be necessary, for example, if some data managers were for any reason unable to carry out the required transaction processing. Whatever decision is made, all data managers must make the same decision in order to preserve the consistency of the database.

Reaching the type of agreement needed for the "commit" problem is straightforward if the participating processes and the network are completely reliable. However, real systems are subject to a number of possible faults such as process crashes, network partitioning, and lost, distorted or duplicated messages. One can even consider more Byzantine types of failure [DS2, DLM, DFFLS, FL, LFF, LSP, PSL] in which faulty processes might go completely haywire, perhaps even sending messages according to some malevolent plan. One therefore wants an agreement protocol which is as reliable as possible in the presence of such faults. Of course, any protocol can be overwhelmed by faults that are too frequent or too severe, so the best that one can hope for is a protocol which is tolerant to a prescribed number of "expected" faults.

In this paper, we show the surprising result that no completely asynchronous consensus protocol can tolerate even a single unannounced process death. We do not consider Byzantine failures, and we assume that the message system is reliable — it delivers all messages correctly and exactly once. Nevertheless, even with these assumptions, the stopping of a single process at

an inopportune time can cause any distributed commit protocol to fail to reach agreement. Thus, this important problem has no robust solution without further assumptions about the computing environment or still greater restrictions on the kind of failures to be tolerated!

Crucial to our proof is that processing is completely asynchronous, that is, we make no assumptions about the relative speeds of processes nor about the delay time in delivering a message. We also assume that processes do not have access to synchronized clocks, so algorithms based on timeouts, for example, cannot be used. (In particular, the solutions in [DS1] are not applicable.) Finally, we do not postulate the ability to detect the death of a process, so it is impossible for one processes to tell whether another has died (stopped entirely) or is just running very slowly.

Our impossibility result applies to even a very weak form of the consensus problem. Assume every process starts with an initial value in  $\{0, 1\}$ . A nonfaulty process decides on a value in  $\{0, 1\}$  by entering an appropriate decision state. All nonfaulty processes which decide are required to choose the same value. For the purpose of the impossibility proof, we require only that some process eventually make a decision. (Of course, any algorithm of interest would require that all nonfaulty processes make a decision.) The trivial solution in which, say, 0 is always chosen is ruled out by stipulating that both 0 and 1 are possible decision values, although perhaps for different initial configurations.

Our system model is rather strong so as to make our impossibility proof as widely applicable as possible. Processes are modelled as automata (with possibly infinitely many states) which communicate by means of messages. In one atomic step, a process can attempt to receive a message, perform local computation based on whether or not a message was delivered to it and if so on which one, and send an arbitrary but finite set of messages to other processes. In particular, an "atomic broadcast" capability is assumed, so a process can send the same message in one step to all other processes with the knowledge that if any nonfaulty process receives the message, then all the nonfaulty processes will. Every message is eventually delivered as long as the destination process makes infinitely many attempts to receive, but messages can be delayed arbitrarily long and delivered out of order.

The asynchronous commit protocols in current use all seem to have a "window of vulnerability" — an interval of time during the execution of the algorithm in which the delay or inaccessibility of a single process can cause the entire algorithm to wait indefinitely. It follows from our impossibility result that every commit protocol has such a "window", confirming a widely-believed tenet in the folklore.

### 2. Consensus Protocols

A consensus protocol P is an asynchronous system of N processes ( $N \ge 2$ ). Each process p has a one-bit input register  $x_p$ , an output register  $y_p$  with values in  $\{b, 0, 1\}$ , and an unbounded amount of internal storage. The values in the input and output registers together with the program counter and internal storage comprise the internal state. Initial states prescribe fixed starting values for all but the input register; in particular, the output register starts with value b. The states in which the output register has value 0 or 1 are distinguished as being decision states. p acts deterministically according to a transition function. The transition function cannot change the value of the output register once the process has reached a decision state; that is, the output register is "write-once". The entire system P is specified by the transition functions associated with each of the processes and the initial values of the input registers.

Processes communicate by sending each other messages. A message is a pair (p, m), where p is the name of the destination process and m is a "message value" from a fixed universe M. The message system maintains a multiset, called the message buffer, of messages that have been sent but not yet delivered. It supports two abstract operations:

send(p, m): places (p, m) in the message buffer;

receive(p): Geletes some message (p, m) from the buffer and returns m, in which case we say (p, m) is delivered, or returns the special null marker  $\phi$  and leaves the buffer unchanged.

Thus, the message system acts nondeterministically, subject only to the condition that if receive(p) is performed infinitely many times, then every message (p, m) in the message buffer is eventually delivered. In particular, the message system is allowed to return  $\phi$  a finite number of times in response to receive(p) even though a message (p, m) is present in the buffer.

is injuration of the system consists of the internal state of each process together with the contents of the message buffer. An initial configuration is one in which each process starts at an initial state and the message buffer is empty.

A step takes one configuration to another and consists of a primitive step by a single process p. Let C be a configuration. The step occurs in two phases. First, receive(p) is performed on the message buffer in C to obtain a value  $m \in M \cup \{\phi\}$ . Then, depending on p's internal state in C and on m, p enters a new internal state and sends a finite set of messages to other processes. Since processes are deterministic, the step is completely determined by the pair e = (p, m), which we call an event. (This "event" should be thought of as the receipt of m by p.) e(C) denotes the resulting configuration and we say that e can be applied to C. Note that the event  $(p, \phi)$  can always be applied to C, so it is always possible for a process to take another step.

A schedule from C is a finite or infinite sequence  $\sigma$  of events which can be applied, in turn, starting from C. The associated sequence of steps is called a run. If  $\sigma$  is finite, we let  $\sigma(C)$  denote the resulting configuration, which is said to be reachable from C. A configuration reachable from some initial configuration is said to be accessible. Hereafter, all configurations mentioned are assumed to be accessible.

The following lemma expresses a "commutativity" property of schedules.

Lemma 1. Suppose that from some configuration C the schedules  $\sigma_1$ ,  $\sigma_2$  lead to configurations  $C_1$ ,  $C_2$  respectively. If the sets of processes taking steps in  $\sigma_1$  and  $\sigma_2$  respectively are disjoint, then  $\sigma_2$  can be applied to  $C_1$  and  $\sigma_1$  can be applied to  $C_2$ , and both lead to the same configuration  $C_3$ . (See Figure 1.)

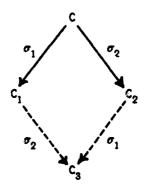


Figure 1.

**Proof.** The result follows at once from the system definition since  $\sigma_1$  and  $\sigma_2$  do not interact.

A configuration C has decision value v if some process p is in a decision state with  $y_p = v$ . A consensus protocol is partially correct if it satisfies two conditions:

- 1. No accessible configuration has more than one decision value.
- 2. For each  $v \in \{0, 1\}$ , some accessible configuration has decision value v.

A process p is nonfaulty in a run provided it takes infinitely many steps, and is faulty otherwise. A run is admissible provided at most one process is faulty, and provided all messages sent to nonfaulty processes are eventually received.

A run is a deciding run provided some process reaches a decision state in that run. A consensus protocol P is totally correct in spite of one fault if it is partially correct, and every admissible run is a deciding run. Our main theorem shows that every partially correct protocol

for the consensus problem has some admissible run which is not a deciding run.

### 3. Main Result

Theorem I. No consensus protocol is totally correct in spite of one fault.

**Proof.** Assume to the contrary that P is a consensus protocol which is totally correct in spite of one fault. We prove a sequence of lemmas which eventually lead to a contradiction.

The basic idea is to show circumstances under which the protocol remains forever indecisive. This involves two steps. First, we argue that there is some initial configuration in which the decision is not already predetermined. Secondly, we construct an admissible run which avoids ever taking a step that would commit the system to a particular decision.

Let C be a configuration and let V be the set of decision values of configurations reachable from C. C is bivalent if |V| = 2. C is univalent if |V| = 1, let us say 0-valent or 1-valent according to the corresponding decision value. By the total correctness of P, and the fact that these are always admissible runs,  $V \neq \phi$ .

### Lemma 2. P has a bivalent initial configuration.

**Proof.** Assume not. Then P must have both 0-valent and 1-valent initial configurations by the assumed partial correctness. Let us call two initial configurations adjacent if they differ only in the initial value  $x_p$  of a single process p. Any two initial configurations are joined by a chain of initial configurations, each adjacent to the next. Hence, there must exist a 0-valent initial configuration  $C_0$  adjacent to a 1-valent initial configuration  $C_1$ . Let p be the process in whose initial value they differ.

Now consider some admissible deciding run from  $C_0$  in which process p takes no steps, and let  $\sigma$  be the associated schedule. Then  $\sigma$  can be applied to  $C_1$  also, and corresponding configurations in the two runs are identical except for the internal state of process p. It is easily shown that both runs eventually reach the same decision value. If the value is 1, then  $C_0$  is bivalent; otherwise,  $C_1$  is bivalent. Either case contradicts the assumed nonexistence of a bivalent initial configuration.

Lemma 3. Let C be a bivalent configuration of P, and let e = (p, m) be an event which is applicable to C. Let C be the set of configurations reachable from C without applying e, and let  $D = e(C) = \{e(E) | E \in C \text{ and } e \text{ is applicable to } E\}$ . Then D contains a bivalent configuration.

**Proof.** Since e is applicable to C, then by definition of C and the fact that messages can be

delayed arbitrarily, e is applicable to every  $E \in C$ .

Now assume that D contains no bivalent configurations, so every configuration  $D \in D$  is univalent. We proceed to derive a contradiction.

Let  $E_i$  be an i-valent configuration reachable from C, i = 0, 1. ( $E_i$  exists since C is bivalent.) If  $E_i \in C$ , let  $F_i = e(E_i) \in D$ . Otherwise, e was applied in reaching  $E_i$ , and so there exists  $F_i \in D$  from which  $E_i$  is reachable. In either case,  $F_i$  is i-valent since  $F_i$  is not bivalent (by assumption) and one of  $E_i$  and  $F_i$  is reachable from the other. Since  $F_i \in D$ , i = 0, 1, D contains both 0-valent and 1-valent configurations.

Call two configurations neighbors if one results from the other in a single step. By an easy induction, there exist neighbors  $C_0$ ,  $C_1 \in C$  such that  $D_i = e(C_i)$  is i-valent, i = 0, 1. Without loss of generality,  $C_1 = e'(C_0)$  where e' = (p', m').

CASE 1: If  $p' \neq p$ , then  $D_1 = e'(D_0)$  by Lemma 1. This is impossible since any successor of a 0-valent configuration is 0-valent. (See Figure 2.)

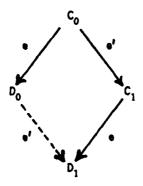


Figure 2.

CASE 2: If p' = p, then consider any finite deciding p-free run from  $C_0$  with corresponding schedule  $\sigma$ , and let  $A = \sigma(C_0)$ . By Lemma 1,  $\sigma$  is applicable to  $D_i$ , and it leads to an i-valent configuration  $E_i = \sigma(D_i)$ , i = 0, 1. Also by Lemma 1,  $e(A) = E_0$  and  $e(e'(A)) = E_1$ . (See Figure 3.) Hence, A is bivalent, which is impossible since A is univalent.

In each case, we reached a contradiction, so D contains a bivalent configuration.

Any deciding run from a bivalent initial configuration goes to a univalent configuration, so there must be some single step which goes from a bivalent to a univalent configuration. Such a step determines the eventual decision value. We now show that it is always possible to run the system in a way that avoids such steps, leading to an admissible non-deciding run.

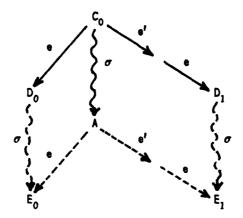


Figure 3.

The run is constructed in stages, starting from an initial configuration. We ensure that the run is admissible in the following way. A queue of processes is maintained, initially in an arbitrary order, and the message buffer in a configuration is ordered according to the time the messages were sent, earliest first. Each stage consists of one or more process steps. The stage ends with the first process in the process queue taking a step in which, if its message queue was not empty at the start of the stage, its earliest message is received. This process is then moved to the back of the process queue. In any infinite sequence of such stages every process takes infinitely many steps and receives every message sent to it. The run is therefore admissible. Our problem of course is to do this in such a way as to avoid a decision ever being reached.

Let  $C_0$  be a bivalent initial configuration whose existence is assured by Lemma 2. Execution begins in  $C_0$ , and we ensure that every stage begins from a bivalent configuration. Suppose then that configuration C is bivalent and that process p heads the priority queue. Let m be the earliest message to p in C's message buffer, if any, and  $\phi$  otherwise. Let e = (p, m). By Lemma 3, there is a bivalent configuration C' reachable from C by a schedule in which e is the last event applied. The corresponding sequence of steps defines the stage.

Since each stage ends in a bivalent configuration, every stage in the construction of the infinite schedule succeeds. The resulting run is admissible, and no decision is ever reached. It follows that P is not totally correct.

### 4. Initially Dead Processes

In this section, we exhibit a protocol which solves the consensus problem for N processes as long as a majority of the processes are non-faulty and no process dies during the execution of the protocol. No process knows in advance, however, which of the processes are initially dead and which are not.

The protocol works in two stages. During the first stage, the processes construct a directed graph G with a node corresponding to each process. Every process broadcasts a message containing its process number and initial value and then listens for messages from L-1 other processes, where  $L = \lceil (N+1)/2 \rceil$ . G has an edge from i to j iff j receives a message from i. Thus, G has indegree L-1.

In the second stage, the processes construct  $G^+$ , the transitive closure of G, in the sense that upon completion of this stage, each process k knows about all of the edges (j, k) incident on k in  $G^+$ . Each k also knows the initial values of all such j. After k discovers such an edge in  $G^+$ , we say that k knows about that edge and about the node j.

The computation of G<sup>+</sup> is carried out in the following way. First, each process broadcasts to all other processes its process number and initial value together with the names of the L-1 processes it heard from during the first stage. It then waits until it has received both the stage 1 and stage 2 messages from all its ancestors in G which it knows about. It initially knows only about the L-1 processes from which it heard directly during the first stage, but as it receives stage 2 messages, it may discover additional ancestors. Waiting continues until such time as all currently known about processes have been heard from.

At this point, each process knows all of its own ancestors and 'he edges of G incident on them, so it can compute all of the edges of G<sup>+</sup> incident on each of its ancestors. This enables it to determine which of its ancestors belong to an initial clique of G<sup>+</sup>, that is, a clique with no incoming edges, for node k is in an initial clique iff k is itself an ancestor of every one of its ancestors. Since every node in G<sup>+</sup> has at least L-1 predecessors, there can be only one initial clique, it has cardinality at least L, and every process which completes the second stage knows exactly the set of processes comprising it.

Finally, each process makes a decision based on the initial values of the processes in the initial clique using any agreed-upon rule. Since all processes know the initial values of all members of the initial clique, they all reach the same decision.

The correctness of this protocol proves the following theorem.

Theorem II. There is a partially correct consensus protocol in which all nonfaulty processes always reach a decision, provided no processes die during its execution and a

strict majority of the processes are alive initially.

### Acknowledgement

The authors would like to thank John Guttag for helpful discussions during the initial phase of this work, and Gene Stark for discussion of the results and a careful reading of the text.

### References

- [DFFLS] Doley, D., Fischer, M., Fowler, R., Lynch, N. and Strong, R. Efficient Byzantine Agreement Without Authentication. In preparation.
  - [DLM] DeMillo, R., Lynch, N. and Merritt, M. Cryptographic Protocols. Proc. 14th ACM Symp. on Theory of Computing (1982), 383-400.
  - [DS1] Doley, D. and Strong, R. Distributed Commit With Bounded Waiting. Proc. 2nd Annual IEEE Symposium on Reliability in Distributed Software and Database Systems (1982).
  - [DS2] Dolev, D. and Strong, R. Polynomial Algorithms for Byzantine Agreement. Proc. 14th ACM Symp. on Theory of Computing (1982), 401-407.
  - [FL] Fischer, M. and Lynch, N. A Lower Bound for the Time to Assure Interactive Consistency. Information Processing Letters 14, 4 (1982), 183-186.
  - [G] Garcia-Molina, H. Elections in a Distributed Computing System. *IEEE Transactions on Computers Vol. C-31*, No. 1 (1982).
  - [LFF] Lynch, N., Fischer, M. and Fowler, R. A Simple and Efficient Byzantine Generals Algorithm. Proc. 2nd Annual IEEE Symposium on Reliability in Distributed Software and Database Systems (1982).
    - [La] Lampson, B. Replicated Commit. CSL Notebook Entry, Xerox Palo Alto Research Center (1981).
    - [Le] LeLann. G. Private communication, quoted in [La].
    - [Li] Lindsay, B. et al. Notes on Distributed Databases. IBM Research Report RJ2571 (1979).
    - [LS] Lampson, B. and Sturgis, H. Crash Recovery in a Distributed Data Storage System. Xerox Palo Alto Research Center Manuscript (1979).
  - [LSP] Lamport, L., Shostak, R. and Pease, M. The Byzantine Generals Problem. ACM Transactions on Programming Languages and Systems 4, 3 (1982), 382-401.
  - [PSL] Pease, M., Shostak, R. and Lamport, L. Reaching Agreement in the Presence of Faults. J. ACM 27, 2 (1980), 228-234.
    - [R] Reed, D. Naming and Synchronization in a Decentralized Conputer System. Ph.D. Thesis, Massachusetts Institute of Technology. Technical Report MIT/LCS/TR-205 (1978).

- [RSL] Rosenkrantz, D., Stearns, R. and Lewis, P. System Level Concurrency Control for Distributed Database Systems. ACM Transactions on Database Systems 3, 2 (1978), 178-198.
  - [S] Skeen. D. A Decentralized Termination Protocol. (Proc. 2nd Annual IEEE Symposium on Reliability in Distributed Software and Database Systems (1982) 27-32.
  - [SS] Skeen. D. and Stonebraker, M. A Formal Model of Crash Recovery in a Distributed Database Systems. Proc. 5th Berkeley Workshop on Distributed Data Management and Computer Networks (1981), 129-142.

### DISTRIBUTION LIST

Office of Naval Research Contract N00014-82-K-0154 Michael J. Fischer, Principal Investigator

Defense Technical Information Center Building 5, Cameron Station Alexandria, VA 22314 (12 copies)

Office of Naval Research 800 North Quincy Street Arlington, VA 22217

Dr. R.B. Grafton, Scientific
Officer (1 copy)
Information Systems Program (437)
(2 copies)
Code 200 (1 copy)
Code 455 (1 copy)
Code 458 (1 copy)

Office of Naval Research Branch Office, Pasadena 1030 East Green Street Pasadena, CA 91106 (1 copy)

Naval Research Laboratory Technical Information Division Code 2627 Washington, D.C. 20375 (6 copies)

Office of Naval Research

Resident Representative
715 Broadway, 5th floor
New York, N.Y. 10003
(1 copy)
Dr. A.L. Slafkosky
Scientific Advisor
Commandant of the Marine Corps
Code RD-1
Washington, D.C. 20380
(1 copy)

Naval Ocean Systems Center Advanced Software Technology Division Code 5200 San Diego, CA 92152 (1 copy)

Mr. E.H. Gleissner Naval Ship Research and Development Center Computation and Mathematics Department Bethesda, MD 20084 (1 copy)

Captain Grace M. Hopper (008)
Naval Data Automation Command
Washington Navy Yard
Building 166
Washington, D.C. 20374
(1 copy)

Defense Advance Research Projects Agency ATTN: Program Management/MIS 1400 Wilson Boulevard Arlington, VA 22209 (3 copies)

Professor Nancy A. Lynch (NE43-525) M.I.T. Laboratory for Computer Science 545 Technology Square Cambridge, MA 02139 (1 copy)

Professor Michael S. Paterson Department of Computer Science University of Warwick Coventry, Warwickshire CV4 7 AL England (1 copy)

# DATE